

**B.Sc. 3rd Semester (Honours) Examination, 2019-20****PHYSICS****Course ID : 32411****Course Code : SH/PHS/301/C-5****Course Title : Mathematical Physics-II****Time: 1 Hours 15 Minutes****Full Marks: 25***The figures in the margin indicate full marks.**Candidates are required to give their answers in their own words as far as practicable.***Section-I**Answer *any five* questions.

1×5=5

1. (a) State Cauchy's Residue theorem.
- (b) Evaluate  $\int_{-\infty}^{\infty} x \delta(x - 4) dx$ .
- (c) Find the nature of the singularity of the function  
 $f(z) = e^{\frac{1}{z-2}}$  at  $z = 2$ .
- (d) What do you mean by unitary matrix?
- (e) Find the probability of drawing 2 aces in succession from a pack of 52 cards.
- (f) Show that if a given co-ordinate is cyclic in the Lagrangian, it will also be cyclic in Hamiltonian.
- (g) What are the properties of eigenvector and eigenvalues of Hermitian matrix?
- (h) What do you mean by a pole?

**Section-II**Answer *any two* questions.

5×2=10

2. (a) Prove that, if  $\hat{A}$  is a linear operator and is invertible then  $\hat{A}^{-1}$  is also a linear operator.
- (b) Define the norm of a vector in linear vector space. What are their properties? 2+3=5
3. (a) Show that every diagonal element of a skew-Hermitian matrix is either zero or a pure imaginary number.
- (b) Given  $A = \begin{bmatrix} 0 & 1 + 2i \\ -1 + 2i & 0 \end{bmatrix}$   
 Show that  $U = [I - A][I + A]^{-1}$  is unitary. 2+3=5

4. If the probability of a bad reaction from a medicine is 0.001, determine the chance that out of 2000 individuals more than two will get a bad reaction. 5
5. Derive canonical equation of motion from variational principle. 5

### Section-III

Answer *any one* question.

10×1=10

6. (a) Find the square root of  $i$ .

(b) Using residue theorem evaluate  $I = \int_{-\infty}^{\infty} \frac{dx}{1+x^2}$

4+6=10

7. (a) Solve the following equations by matrix method

$$\begin{aligned} x - 2y + 3z &= 5 \\ 4x + 3y + 4z &= 7 \\ x + y - z &= -4 \end{aligned}$$

- (b) Are the following vectors linearly dependent or not?

$$\begin{aligned} x_1 &= (3, 2, 7) \\ x_2 &= (2, 4, 1) \\ x_3 &= (1, -2, 6) \end{aligned}$$

- (c) Show that

(i)  $\delta[c(x - a)] = \frac{1}{|c|} \delta(x - a)$

(ii)  $\delta[(x^2 - a^2)] = \frac{1}{2a} [\delta(x - a) + \delta(x + a)], a > 0$

5+2+3=10

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